

List of Publications of Thomas F. Banchoff

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- [21] Height functions with three critical points (with Floris Takens), Illinois J. Mathematics, 76 (1975), 325-335.
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- [24] Immersions and Mod 2 Quadratic Forms (with Lou Kauffman), American Mathematical Monthly 84 (1977), 168-185. (Awarded Lester Ford Award for exposition, Summer 1978).
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