

1. Evaluate the integral  $\int (x \ln x)^2 dx$ .
2. Evaluate the integral  $\int \sin^2 5x \cos^2 5x dx$ .
3. Evaluate the integral  $\int_0^1 \frac{e^{2x}}{e^{2x} + 1} dx$ .
4. Evaluate the integral  $\int \frac{5x^3 + 2x^2 - 12x - 8}{x^4 - 8x^2 + 16} dx$ .
5. Evaluate the integral  $\int \frac{1}{x\sqrt{4 - 9x^2}} dx$ .
6. Determine whether or not the improper integral converges. If it converges, find its value.

$$\int_0^\pi \sec^2 x dx$$

ANSWERS:

1.  $\frac{x^3(\ln x)^2}{3} - \frac{2x^3 \ln x}{9} + \frac{2x^3}{27} + C$
2.  $\frac{x}{8} - \frac{\sin 20x}{160} + C$
3.  $\frac{1}{2} \ln\left(\frac{e^2+1}{2}\right)$
4.  $-\frac{1}{x-2} + 3 \ln|x-2| + \frac{1}{x+2} + 2 \ln|x+2| + C$
5.  $-\frac{1}{2} \ln\left|\frac{2}{3x} + \frac{\sqrt{4-9x^2}}{3x}\right| + C$
6. The integral is divergent.